Structural Model	Counterfactual Experiments	Conclusion

# Decentralized decision-making in retail chains: Evidence from inventory management

Victor Aguirregabiria (University of Toronto & CEPR) Francis Guiton (University of Toronto)

IIOC 2022 - May 14, 2022

Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail che</mark> IIOC 2022 – May 14, 2022 1/23

Introduction	Structural Model	Counterfactual Experiments	Conclusion
•0000			

## This paper deals with:

- Allocation of decision rights within multi-division firms; trade-offs in this allocation; & implications on firm performance.
- More specifically, it deals with **inventory management in the stores** of large retail chain, and the choice between:
  - Centralized inventory management controlled at headquarters
  - Or **Decentralized system** where each local store manager chooses what and when to order for her store.
- A main trade-off: Just-in-time information available to store managers; but store managers are heterogeneous in their skills.

# Setting: Liquor Control Board of Ontario (LCBO)

- Second largest buyer/seller of liquor in the world.
- In 2021: CAD 7.18 B revenue; CAD 2.54 B profit (net income);
   677 stores; > 22K products; > 10K employees.
- Centralized pricing system: Uniform pricing across all the stores.
- Decentralized inventory management:

- HQs use store-level sales data to make ordering recommendations to each store. Recommendations are sent 1 week after the sales data.

イロト 不得下 イヨト イヨト

- 3

- Local store managers make daily replenishment decisions and can (do) deviate from HQs recommendations.

 Introduction
 Structural Model
 Estimation
 Counterfactual Experiments
 Conclusion

 00000
 000
 0000
 000
 00
 00

# Empirical strategy / Empirical results [1/2]

- 1. Daily data at store-product level on sales, prices (retail & wholesale), orders, inventories, stockouts for every product & store over 676 days.
- 2. Estimation of **reduced form (S,s) inventory model** separately for each store shows large store heterogeneity in inventory decisions.
- Estimation of a structural model of inventory decisions separately for each store – shows substantial store heterogeneity in structural parameters: fixed ordering costs, and per unit storage costs, stockout costs, and ordering costs.
- 4. A very substantial part of store heterogeneity in cost parameters cannot be explained by a rich set of store and location characteristics: it seems idiosyncratic of store managers.

 Introduction
 Structural Model
 Estimation
 Counterfactual Experiments
 Conclusion

 000
 000
 0000
 000
 00
 00

# Empirical strategy / Empirical results [2/2]

Using the estimated model, we implement **counterfactual experiments**.

5. Removing store managers' idiosyncratic heterogeneity

- Substantial reduction in ordering frequency and inventory-to-sales ratio, but negligible effect on the frequency of stockouts.

- If the idiosyncratic component of costs is a biased perception by store managers, then it has a substantial negative effect on the firm's profit.

#### 6 Centralizing the decision-making of inventory management.

- Modest (0.4%) increase in annual profit for LCBO. The result of combining two large effects with opposite signs.

- Delay in forecasting demand has negative impact on profits but it is more than compensated by positive effect from removing store managers' heterogeneity.

5/23

Introduction	Structural Model	Counterfactual Experiments	Conclusion
00000			

#### Related Literature

# 1. Empirical research on allocation of decision rights in multi-division firms

DellaVigna & Gentzkow (2019); Hortaçsu et al. (2021); Bloom, Sadun & Van Reenen (2012); Alfaro, Bloom et al. (2019); ...

#### 2. Structural models of firms' inventory decisions:

Hall & Rust (2000); Kryvtsov & Midrigan (2013); Bray et al. (2019, 2021);

#### 2. Structural models of firm behaviour with manager biases:

Goldfarb and Xiao (2011), Ellison, Snyder and Zhang (2018), Goldfarb and Xiao (2019); ...

A (10) A (10)

- 3

Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail cha</mark> IIOC 2022 – May 14, 2022 6/23

Structural Model	Counterfactual Experiments	Conclusion
•00		

# Structural Model: Sequence of Events [1/2]

- Step (i): Day t begins with store manager observing: current stock (k<sub>t</sub>); price-cost margin (p<sub>t</sub> c<sub>t</sub>); demand shifters (z<sub>t</sub>) that determine mean and variance of log-demand: (ln d<sup>e</sup>(z<sub>t</sub>) and σ<sup>2</sup>(z<sub>t</sub>)); ordering cost shock (ε<sub>t</sub>).
- Step (ii): Store manager orders yt ∈ {0, 1, ..., J} units of inventory. It takes one day for an order to be delivered to the store.
- Step (iii): Demand d<sub>t</sub> is realized with Negative Binomial distrib.
   Units sold q<sub>t</sub> are the minimum of supply and demand:

$$q_t = \min\{ d_t, k_t \}$$

(日本)(日本)(日本)(日本)

Structural Model	Counterfactual Experiments	Conclusion
000		

# Structural Model: Sequence of Events [2/2]

• Step (iv): The store generates flow profits Π<sub>t</sub> =

 $(\mathsf{p}_t - c_t) \min\{d_t, k_t\} - \gamma^z \mathbb{1}\{d_t > k_t\} - \gamma^h k_t - \gamma^c y_t - \gamma^f \mathbb{1}\{y_t > 0\} + \sigma_{\varepsilon}\varepsilon_t(\mathbf{x}_t) + \sigma_{\varepsilon}\varepsilon_t(\mathbf{x}_t$ 

 $\gamma^{z} = \text{Per unit stockout cost};$   $\gamma^{h} = \text{Per unit storage cost};$   $\gamma^{c} = \text{Per unit ordering cost};$   $\gamma^{f} = \text{Fixed ordering cost};$  $\sigma_{\varepsilon} = \text{Std. dev. of transitory shock in order costs}$ 

• Step (v) Orders arrive to the store, and inventory is updated:

$$k_{t+1} = k_t + y_t - q_t$$

Next period price (and margin) is realized from  $F_p(p_{t+1}|p_t)$ .

Structural Model	Counterfactual Experiments	Conclusion
000		

#### Dynamic Programming Problem

- A store manager chooses the order quantity y<sub>t</sub> to maximize her store's expected and discounted stream of current and future profits.
- This is a dynamic programming (DP) problem with state variables  $\mathbf{x}_t \equiv (\mathbf{z}_t, k_t, p_t c_t)$  and  $\varepsilon_t$ , and Bellman equation:

 $V(\boldsymbol{x}_t, \boldsymbol{\varepsilon}_t) = \max_{y_t \in \mathcal{Y}} \{ \pi(y_t, \boldsymbol{x}_t) + \sigma_{\varepsilon} \varepsilon(y_t) + \beta \mathbb{E} [V(\boldsymbol{x}_{t+1}, \boldsymbol{\varepsilon}_{t+1}) \mid y_t, \boldsymbol{x}_t] \}$ 

イロト 不得 とくき とくき とうき

• Each store-product has its own demand and cost parameters and its own DP problem.

Victor Aguirregabiria (University of TororDecentralized decision-making in retail cha IIOC 2022 – May 14, 2022 9/23

Introduction 00000	Structural Model	Estimation ●0000000	Counterfactual Experiments	Conclusion

#### Estimation

- For each of the 634 stores in the chain and each product in our working sample, we estimate:
  - Demand parameters in functions  $\ln d^e(\mathbf{z}_t)$  and  $\sigma^2(\mathbf{z}_t)$ ;
  - Cost parameters:

$$\boldsymbol{\gamma} = (\sigma, \gamma^h, \gamma^z, \gamma^f, \gamma^c)'$$

• We estimate demand parameters in a first step, and then cost parameters using a Sequential Pseudo Maximum Likelihood method (Aguirregabiria and Mira, 2002).

Structural Model	Estimation	Counterfactual Experiments	Conclusion
	0000000		

#### Structural Estimates of Cost Parameters (in CAD)

	Median	Std. Dev.	Median	Median
	Estimate	Estimate	S.e.	t-stat.
$\gamma^{h}$ : Per unit Storage Cost	0.0040	0.0031	0.0008	5.2331
$\gamma^{z}$ : Stockout Cost	0.0179	0.3433	0.1477	0.2545
$\gamma^{\it f}$ : Fixed Ordering Cost	2.9626	1.1403	0.2403	12.3417
$\gamma^{c}$ : Per-Unit Ordering Cost	0.0336	0.0697	0.0285	1.4282
# store-product pairs	3,076			

Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail cha</mark> IIOC 2022

IIOC 2022 - May 14, 2022 11/23



#### Store Heterogeneity in Storage Cost (Shrinkage Estimator)

Figure:  $\gamma^h$ 



IIOC 2022 - May 14, 2022 12/23



#### Store Heterogeneity in Stockout Cost (Shrinkage Estimator)

Figure:  $\gamma^z$ 



Victor Aguirregabiria (University of TororDecentralized decision-making in retail cha IIOC 2022 – May 14, 2022 13/23



#### Store Heterogeneity in Fixed Ord Cost (Shrinkage Estimator)

Figure:  $\gamma^{f}$ 



Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail che</mark> IIOC 2022 – May 14, 2022 14/23



#### Store Heterogeneity in Unit Ord Cost (Shrinkage Estimator)

Figure:  $\gamma^c$ 



## Contribution of Inventory Costs to Profits

Table: Realized Inventory Management Costs to Revenue Ratios

	Median	St. Dev.
Inventory Holding Cost to Revenue Ratio (%) Stockout Cost to Revenue Ratio (%) Fixed Ordering Cost to Revenue Ratio (%) Variable Ordering Cost to Revenue Ratio (%)	0.3219 0 0.8677 0.2034	0.2139 0.0079 0.7203 0.1951
Total Inventory Cost to Revenue Ratio (%)	1.4903	0.8451

< □ > < 同 > < 回 > < 回 > < 回 >

3

## Regression for Estimated Costs on Store Characteristics

Table: Regression of Cost Parameters on Store and Location Characteristics



## Counterfactual: Centralized Decision Making [1/4]

- Centralizing decision making entails a trade-off between eliminating potential managerial biases and losing valuable store-level information.
- 1. Based on the own firm's reports, we assume that in the centralized system, predictions about demand at the store level are generated with one week delay.
- 2. We assume that the residual component (from regression on store characteristics) in store costs is not an actual cost but managerial bias.

< □ > < 同 > < 回 > < 回 > < 回 >

# Counterfactual: Centralized Decision Making [2/4]

**Table:** Decentralized vs.Centralized Profits: Average Daily Profit Per-StorePer-Product (in CAD)

	Mean	P 10%	P 25%	Median	P 75%	P 90%
Centralized Solution (\$)	54.93	9.75	18.28	43.91	82.21	116.13
Decentralized Solution (\$)	54.64	9.75	18.15	44.01	81.92	116.35
Gains in Profit from Decentralization (\$)	-0.29	-2.29	-1.01	-0.20	0.26	1.45
Gains in Profit from Decentralization (%)	-0.41	-3.52	-2.26	-0.73	1.02	3.27
Change Inventory Cost from Decentralization (%)	25.45	-5.52	0.10	6.30	23.01	56.97

1% change in profit per store-product is approximately \$17 million in total annual profit for LCBO.



#### Counterfactual: Centralized Decision Making [3/4]

Figure: Change in Daily Profit From Decentralization (\$)



20 / 23

Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail cha</mark> IIOC 2022 – May 14, 2022



#### Counterfactual: Centralized Decision Making [4/4]

Figure: Change in Daily Inventory Cost From Decentralization (%)



Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail che</mark> IIOC 2022 – May 14, 2022 21 / 23

Introduction 00000	Structural Model	Estimation 00000000	Counterfactual Experiments	Conclusion ●○
Conclusion	[1/2]			

- Retail chains are complex organizations with multiple divisions and teams, each with its own decision rights.
- Store managers play an important role in retail chains.
- Store managers can collect and process information just-in-time about their own stores. Processing this store level information at HQs can generate delays of days or even weeks.
- On the other hand, store managers can have heterogeneous skills, motivations, and can put different levels of effort.
- We investigate this trade-off in the context of inventory management in a large retail chain.

Victor Aguirregabiria (University of Toror<mark>Decentralized decision-making in retail chaal IIOC 2022 –</mark> May 14, 2022 22 / 23

Introduction 00000	Structural Model	Estimation 00000000	Counterfactual Experiments	Conclusion ○●
Conclusion	[2/2]			

- We find that a centralized inventory management system would yield a 0.4% increase in annual profit.
- This modest effect is the result of combining two substantial effects with opposite signs.

- A negative impact on profits of losing the *just-in-time* information from store managers.

- A large reduction in ordering and storage costs from eliminating store managers' behavioral biases and heterogeneous skills.

• The gains/losses from centralization are very heterogeneous across stores in the retail chain.